

2019 Spring Semester Quiz 1
For General Chemistry I (CH101)

Date: Mar 18 (Mon), Time: 19:00 ~ 19:45

Professor Name	Class	Student I.D. Number	Name

Use the following constants to solve problems. The periodic table is given in the last page of this quiz.

(Planck constant $h = 6.626 \times 10^{-34} \text{ J s}$) (Mass of electron $m_e = 9.109 \times 10^{-31} \text{ kg}$)
(Permittivity of the vacuum $\epsilon_0 = 8.854 \times 10^{-12} \text{ C}^2 \text{ J}^{-1} \text{ m}^{-1}$) (Charge of the electron $e = 1.602 \times 10^{-19} \text{ C}$)
(Speed of light $c = 2.998 \times 10^8 \text{ m/s}$) ($\pi = 3.1416$) (Avogadro's number $N_A = 6.022 \times 10^{23}$)

1. (Total 10 pts, 2 pts for each) **Answer the following questions.**

(a) Which atom has the highest ionization energy?

F, Ne, Na, Ar

Answer: _____ **Ne** _____

(b) Which atom is most electronegative?

K, Ca, Br, I

Answer: _____ **Br** _____

(c) Which compound has the most ionic bonding character?

IF, ICl, ClF, BrCl, Cl₂

Answer: _____ **IF** _____

(d) Which electromagnetic radiation has the longest wavelength?

X-ray, microwave, violet light, red light

Answer: _____ **Microwave** _____

(e) Which one has the longest de Broglie wavelength, if they are moving at the same velocity?

Electron, proton, H atom, He atom

Answer: _____ **Electron** _____

2. (Total 8 pts) Consider the ionic compound KCl. The ionization energy (IE) and electron affinity (EA) of potassium and chlorine are as follows:

	K	Cl
IE (kJ/mol)	418.8	1251.1
EA (kJ/mol)	48.384	349.0

(a) (3 pts) Using the given data, explain why K^+Cl^- form in preference to K^-Cl^+ .

$$\Delta E \text{ (for } K^+Cl^-\text{)}(g) = 418.8 + (-349.0) = \boxed{69.8 \text{ kJ mol}^{-1}}$$

$$\Delta E \text{ (for } K^-Cl^+\text{)}(g) = 1251.1 + (-48.384) = \boxed{1202.7 \text{ kJ mol}^{-1}}$$

2 pts for correct calculation or correct explanation (that reaction proceeds in a pathway with lower ΔE)

1 pt for explaining that reaction proceeds with lower energy barrier

b) (5 pts) Estimate the energy of dissociation (ΔE_d) to neutral atoms for KCl , which has a bond length 2.67×10^{-10} m.

$$V_{\text{Coulomb}} = \frac{q_K + q_{Cl^-}}{4\pi\epsilon_0 R_e} = \frac{(+1.602 \times 10^{-19} \text{ C})(-1.602 \times 10^{-19} \text{ C})}{4(3.1416)(8.854 \times 10^{-12} \text{ C}^2 \text{ J}^{-1} \text{ m}^{-1})(2.67 \times 10^{-10} \text{ m})} = -8.64 \times 10^{-19} \text{ J}$$

This potential energy is for one K^+ to Cl^- interaction. For a *mole* of these pair-wise interactions, multiply by Avogadro's number

$$V_{\text{Coulomb}} = (-8.64 \times 10^{-19} \text{ J pair}^{-1}) \times (6.022 \times 10^{23} \text{ pair mol}^{-1}) = -520 \times 10^3 \text{ J mol}^{-1}$$

$$\Delta E_d = -V_{\text{Coulomb}} - \Delta E_{\infty}$$

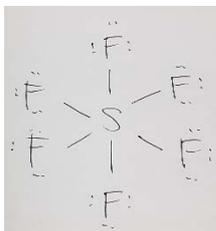
$$= -(-520 \text{ kJ mol}^{-1}) - (418.8 \text{ kJ mol}^{-1} - 349.0 \text{ kJ mol}^{-1}) = \boxed{450 \text{ kJ mol}^{-1}}$$

--- $V_{\text{coulomb}}, \Delta E_d$ +1 pt each

1 pt each for correct equations, 3 pts for the correct answer

3. (Total 8 pts, each 2 pts) **Based on VSEPR theory, draw Lewis diagrams with the smallest formal charges, and name the geometry for given molecules. If there are possible resonance forms, please draw all of them.**

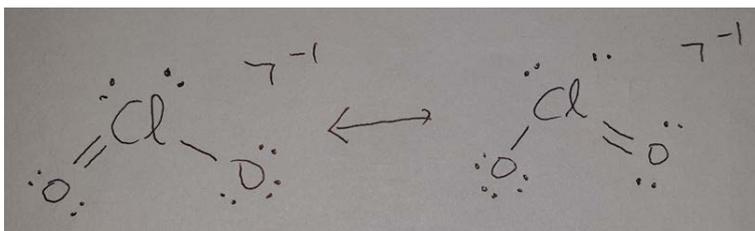
(a) SF_6



Correct Lewis diagram ----- + 1 pt

Geometry: Octahedral ----- + 1 pt

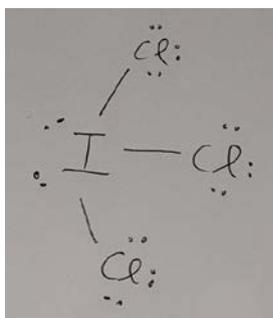
(b) ClO_2^-



0.5 pt for one resonance structure; 0.5 pt for full resonance ----- + 1 pt

Geometry: bent ----- + 1 pt

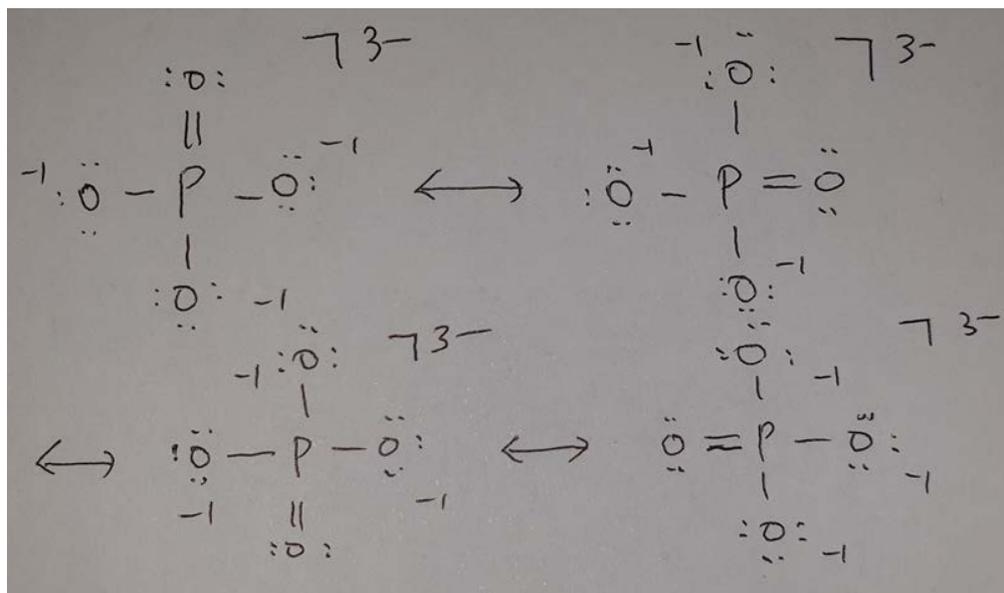
(c) ICl_3



Correct Lewis diagram ----- + 1 pt

Geometry: T-shaped ----- + 1 pt

(d) PO_4^{3-}



0.5 pt for one resonance structure; 0.5 pt for full resonance ----- + 1 pt

Geometry: tetrahedral----- + 1 pt

4. (Total 7 pts) Consider a universe with a different value of the Planck constant. When lithium is irradiated with light in this universe, the kinetic energy of the ejected electrons is 2.935J for $\lambda=300.0\text{nm}$ and 1.280J for $\lambda=400.0\text{nm}$ (λ is the wavelength of the light).

(a) (2 pts) Calculate the Planck constant in this universe.

$$2.935\text{J} = \frac{hc}{\lambda_1} - \phi$$

$$1.280\text{J} = \frac{hc}{\lambda_2} - \phi$$

$$\therefore 2.935\text{J} - 1.280\text{J} = hc \left(\frac{1}{\lambda_1} - \frac{1}{\lambda_2} \right) \dots + 1\text{pt}$$

$$1.655\text{J} = h(2.998 \times 10^8 \text{m} \cdot \text{s}^{-1}) \left(\frac{1}{300 \times 10^{-9}\text{m}} - \frac{1}{400 \times 10^{-9}\text{m}} \right)$$

$$\therefore h = \frac{1.655\text{J}}{2.498 \times 10^{14}\text{s}^{-1}} = 6.625 \times 10^{-15}\text{J} \cdot \text{s} \dots + 1\text{pt}$$

+1 pt for the correct equation, +1 pt for the correct answer

(b) (1 pt) Calculate the work function of lithium in this universe.

$$\phi = \frac{hc}{\lambda_1} - 2.935\text{J} = \frac{(6.625 \times 10^{-15}\text{J}) \times (2.998 \times 10^8 \text{m} \cdot \text{s}^{-1})}{300 \times 10^{-9}\text{m}} - 2.935\text{J} = 3.686\text{J}$$

+1 pt for the correct answer; no partial points

(c) (2 pts) In this universe, what is the maximum kinetic energy of electrons ejected from lithium by the light of wavelength of 200.0 nm?

$$E_{max} = \frac{hc}{\lambda} - \phi = \frac{(6.625 \times 10^{-15} \text{J}) \times (2.998 \times 10^8 \text{m} \cdot \text{s}^{-1})}{200 \times 10^{-9} \text{m}} - 3.686 \text{J} = 6.245 \text{J}$$

+1 pt for the $E_{max} = \frac{hc}{\lambda} - \phi$ equation, +1 pt for the correct answer

(d) (2 pts) Suppose the electrons described in (c) were used in a diffraction experiment. What would be their wavelength in this universe? Use the maximum kinetic energy value from (c).

$$KE = \frac{1}{2} m_e v^2 = \frac{p^2}{2m}$$

$$\therefore p = \sqrt{2m \times KE} \dots + 1 \text{pt}$$

$$\text{de Broglie wavelength } \lambda = \frac{h}{p} = \frac{(6.625 \times 10^{-15} \text{J} \cdot \text{s})}{\sqrt{2 \times 9.109 \times 10^{-31} \text{kg} \times 6.245 \text{J}}} = 1.964 \text{m} \dots + 1 \text{pt}$$

+1 pt for the correct equation, +1 pt for the correct answer

5. (Total 7 pts) Consider an electron in a one-dimensional box with length L , where potential $V = 0$ everywhere inside the box. The solution for the Schrödinger's equation of this system is as follows:

$$\psi_n(x) = \sqrt{\frac{2}{L}} \sin\left(\frac{n\pi x}{L}\right) \quad n = 1, 2, 3, \dots$$

(a) (4 pts) Using the given wavefunction, show that the energy level of this particle in a box is as follows:

$$E_n = \frac{n^2 h^2}{8mL^2} \quad n = 1, 2, 3, \dots$$

To find the energy E_n for a particle described by the wave function ψ_n , we calculate the second derivative:

$$\begin{aligned} \frac{d^2 \psi_n(x)}{dx^2} &= \frac{d^2}{dx^2} \left[\sqrt{\frac{2}{L}} \sin\left(\frac{n\pi x}{L}\right) \right] \\ &= -\left(\frac{n\pi}{L}\right)^2 \left[\sqrt{\frac{2}{L}} \sin\left(\frac{n\pi x}{L}\right) \right] \\ &= -\left(\frac{n\pi}{L}\right)^2 \psi_n(x) \end{aligned}$$

This must be equal to $-\frac{8\pi^2 m E_n}{h^2} \psi_n(x)$. Setting the coefficients equal to one another gives

$$\frac{8\pi^2 m E_n}{h^2} = \frac{n^2 \pi^2}{L^2} \quad \text{or}$$

$$E_n = \frac{n^2 h^2}{8mL^2} \quad n = 1, 2, 3, \dots$$

+1 pt for the correct Schrödinger's equation:

$$-\frac{\hbar^2}{8\pi^2m} \frac{d^2\psi_n(x)}{dx^2} = E\psi_n(x)$$

+2 pts for correct differentiation:

$$\frac{d^2\psi_n(x)}{dx^2} = -\left(\frac{n\pi}{L}\right)^2 \psi_n(x)$$

+1 pt for correct derivation

(b) (3 pts) Suppose the electron is in the ground state. The light with the wavelength of 500 nm excited this electron into the first excited state. What is the length of this box?

$$\Delta E = \frac{\hbar^2}{8mL^2} (2^2 - 1^2) = \frac{3\hbar^2}{8mL^2} = \frac{hc}{\lambda}$$

$$L^2 = \frac{3h\lambda}{8mc} \quad \therefore L = \sqrt{\frac{3h\lambda}{8mc}} \dots + 1pt$$

$$= \sqrt{\frac{3 \times (6.626 \times 10^{-34} \text{J} \cdot \text{s}) \times (500 \times 10^{-9} \text{m})}{8 \times (9.109 \times 10^{-31} \text{kg}) \times (2.998 \times 10^8 \text{m} \cdot \text{s}^{-1})}} = 6.745 \times 10^{-10} \text{m} = 6.745 \text{Å} \dots + 2pt$$

+1 pt for the correct equation, +2 pts for the correct answer

**Any final answer WITHOUT the correct units got 0.5 pt deduction.

